SYLLABUS FOR THE ENTRANCE TEST IN MATHEMATICS, JOINT DEGREES, AND COMPUTER SCIENCE

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- **Polynomials:** The quadratic formula. Completing the square. Discriminant. Factorisation. Factor Theorem.
- Algebra: Simple simultaneous equations in one or two variables. Solution of simple inequalities. Binomial Theorem with positive whole exponent. Combinations and binomial probabilities.
- Differentiation: Derivative of x^a , including for fractional exponents. Derivative of e^{kx} . Derivative of a sum of functions. Tangents and normals to graphs. Turning points. Second order derivatives. Maxima and minima. Increasing and decreasing functions. Differentiation from first principles.
- Integration: Indefinite integration as the reverse of differentiation. Definite integrals and the signed areas they represent. Integration of x^a (where $a \neq -1$) and sums thereof.
- Graphs: The graphs of quadratics and cubics. Graphs of

 $\sin x$, $\cos x$, $\tan x$, \sqrt{x} , a^x , $\log_a x$.

Solving equations and inequalities with graphs.

- Logarithms and powers: Laws of logarithms and exponentials. Solution of the equation $a^x = b$.
- Transformations: The relations between the graphs

$$y = f(ax), \quad y = af(x), \quad y = f(x-a), \quad y = f(x) + a$$

and the graph of y = f(x).

- Geometry: Co-ordinate geometry and vectors in the plane. The equations of straight lines and circles. Basic properties of circles. Lengths of arcs of circles.
- **Trigonometry:** Solution of simple trigonometric equations. The identities

$$\tan x = \frac{\sin x}{\cos x}, \quad \sin^2 x + \cos^2 x = 1, \quad \sin(90^\circ - x) = \cos x.$$

Periodicity of sine, cosine and tangent. Sine and cosine rules for triangles.

- Sequences and series: Sequences defined iteratively and by formulae. Arithmetic and geometric progressions^{*}. Their sums^{*}. Convergence condition for infinite geometric progressions^{*}.
- * Part of full A-level Mathematics syllabus.