The William Rowan Hamilton Geometry and Topology Workshop: Celebrating Martin Bridson's 60th Birthday

### 30 June - 4 July 2025

Joly Theatre, <u>Hamilton Conference Centre</u>, Trinity College, Dublin, Ireland





### **Hamilton Mathematics Institute**

The Hamilton Mathematics Institute (HMI) at Trinity College Dublin was founded in 2005, marking the 200th anniversary of the birth of William Rowan Hamilton - Ireland's greatest mathematician.

### <u>How to find us</u>

Found at the east end of the campus, the Joly Theatre is located in the Hamilton Conference Centre. The Centre is conveniently close to the Trinity Business School and just a short walk from Pearse Street train station.

### Monday, 30 June

0930 - 1020	Alan Reid, Rice Profinite rigidity: past present, future
1030 - 1100	COFFEE
1100 - 1150	Emmanuel Breuillard, Oxford Word maps and character varieties
1200 - 1400	LUNCH
1400 -1450	Koji Fujiwara, Kyoto Well-ordered growth rates in families of groups of negative curvature
1500 - 1550	Tara Brendle, Glasgow The kernel of the Birman-Craggs-Johnson homomorphism
1600 - 1630	BREAK
1630 - 1720	Giles Gardam, Bonn Groups, rings, and geometry

### Tuesday, 1 July

0930 - 1020	Mladen Bestvina, Utah
1030 - 1100	COFFEE
1100 - 1150	Ruth Charney, Brandeis Outer Space for Right-Angled Artin Groups
1200 - 1400	LUNCH
1400 -1450	CLAY LECTURE: Alex Lubotsky, Weizmann Institute From group theory to computer science and back
1500 - 1550	Matthew Stover, Temple University High dimensional hyperbolic Coxeter groups that virtually fiber
1600 - 1630	BREAK
1630 - 1720	Claudio Llosa Isenrich, KIT From geometric group theory to complex geometry (and back)
1600 - 1820	POSTER SESSION 1 Posters displayed from beginning of afternoon coffee break

### Wednesday, 2 July

0900 - 0950	CLAY LECTURE: Karen Vogtmann, Warwick Graphs, surfaces, and handlebodies: markings and boundary complexes
1000 - 1030	COFFEE
1030 - 1120	Dessislava Kochloukova, State University of Campinas Weak commutativity, virtually nilpotent groups, and Dehn functions
1130 - 1220	Richard Schwartz, Brown The optimal paper Moebius band

#### **FREE AFTERNOON**

### Thursday, 3 July

0930 - 1020	Ian Agol, UC Berkeley Hyperbolic lattices as automorphism groups
1030 - 1100	COFFEE
1100 - 1150	Anne Thomas, Sydney Reflections, cubulations and Kazhdan-Lusztig polynomials
1200 - 1400	LUNCH
1400 -1450	Kasia Jankiewicz, UC Santa Cruz Cubical quotients of cubical nonproducts
1500 - 1550	Richard Wade, Oxford Duality for Cohen-Macaulay complexes and the top dimensional cohomology of Out(F_N)
1600 - 1630	BREAK
1630 - 1720	Tatiana Nagnibeda, Geneva Groups acting on rooted trees and their subgroups
1600 - 1830	POSTER SESSION II
1900 - 2200	CONFERENCE BANQUET Trinity College Dining Hall located in front square

### Friday, 4 July

0900 - 0950	<b>Pierre-Emmanuel Caprace, UC Louvain</b> Some BMW groups I have known
1000 - 1030	COFFEE BREAK
1030 - 1120	Jean Pierre Mutanguha, McGill Canonical decompositions of free-by-cyclic groups
1130 - 1220	Wolfgang Lück, Bonn K-theory, groups, and geometry
	END OF CONFERENCE

### Monday, 30 June

#### Alan Reid, Rice *Profinite rigidity: past present, future*

This talk will survey profinite rigidity. This will include a discussion of recent history, some ongoing work as well as posing questions to hopefully stimulate further research in the area.

#### Emmanuel Breuillard, Oxford Word maps and character varieties

I will discuss an on-going project (with O. Becker and P. Varju and with I. Glazer) to study the geometry of generic word maps on semisimple Lie groups, in particular the dimension and regularity of their fibers. The techniques are arithmeticogeometric in nature and the analysis involves uniform expanders in finite quotients. We obtain information on the geometry of character varieties of random groups in the few relators model. The case when the deficiency of the presentation is 1, gives rise to an interesting family of rigid Zariski-dense subgroups.

#### Koji Fujiwara, Kyoto

### Well-ordered growth rates in families of groups of negative curvature

It is known that the set of growth rates of a non-elementary hyperbolic group, over all finite generating sets, is well-ordered. In this talk, I will discuss the set of growth rates that occur in certain families of groups. I will focus on families of hyperbolic manifold groups and 3-manifold groups.

### Tara Brendle, Glasgow

#### The kernel of the Birman-Craggs-Johnson homomorphism

The Torelli group is the subgroup of the mapping class group of a surface that acts trivially on the first homology group of that surface. In the 1980s, Dennis Johnson wrote a series of groundbreaking papers describing the structure of this group, culminating in the calculation of its abelianization. The Birman-Craggs Johnson homomorphism measures the 2-torsion part of this abelianization, via certain 3- and 4-manifold invariants. In this talk, we will describe a simple generating set for the kernel of the Birman--Craggs--Johnson homomorphism, which can then be used to give a new and simpler proof of Johnson's calculation of the abelianization of the Torelli group. This is joint work in progress with Andrew Putman.

#### Giles Gardam, Bonn Groups, rings, and geometry

I will discuss the interplay between groups, their group rings, and their geometry, with emphasis on the Kaplansky conjectures.

### Tuesday, 1 July

Mladen Bestvina, Utah

#### Ruth Charney, Brandeis *Outer Space for Right-Angled Artin Groups*

Culler and Vogtmann's Outer Space has played a central role in the study of automorphism groups of free groups. In joint work with Bregman and Vogtmann, we constructed an analogous space for any right-angled Artin group. In this talk, I will review the construction of this outer space, then discuss some recent (and ongoing) applications of these spaces.

#### CLAY LECTURE: Alex Lubotsky, Weizmann Institute From group theory to computer science and back

We will present several projects in computer science (CS) where group theory is involved and suggest some group-theoretic problems inspired by CS.

#### Matthew Stover, Temple University High dimensional hyperbolic Coxeter groups that virtually fiber

I will describe an iterative procedure, devised jointly with Lafont, Minemyer, Sorcar, and Wells, for constructing hyperbolic Coxeter groups that virtually fiber over  $\mathbb{Z}$ . A topological argument shows that iteration increases virtual cohomological dimension (vcd) by exactly one, and hence produces infinitely many isomorphism classes in each vcd  $n \ge 2$ . Our procedure combines results of Jankiewicz, Norin, and Wise with a generalization of a construction due to Osajda involving a new simplicial thickening process.

#### Claudio Llosa Isenrich, KIT From geometric group theory to complex geometry (and back)

A classical problem in complex algebraic geometry is understanding the topology of closed complex submanifolds of complex projective space, so-called smooth complex projective varieties, and, more generally, of compact Kähler manifolds. Two natural invariants are the fundamental group and its profinite completion; also known as the algebraic fundamental group. I will explain how tools from geometric group theory can be used to understand these invariants and their relation.

In particular, I will address the following question: When is the fundamental group of a compact Kähler manifold (or even its homeomorphism type) uniquely determined by its profinite completion? I will explain a positive answer for direct products of closed non-positively curved Riemann surfaces. This is a consequence of the profinite invariance of the so-called universal morphism of a Kähler group to a direct product of (orbi)surface groups.

Time-permitting, I will indicate how, conversely, complex geometry can be used to solve problems in geometric group theory, with the example of the construction of subgroups of hyperbolic groups with exotic finiteness properties. This talk is based on joint works with Hughes, Py, Stover and Vidussi.

### Wednesday, 2 July

### CLAY LECTURE: Karen Vogtmann, Warwick Graphs, surfaces, and handlebodies: markings and boundary complexes

In Teichmüller space Riemann surfaces are marked by a homeomorphism from a model surface. We define a notion of complex handlebody, which can be marked by either a homeomorphism or a homotopy equivalence from a model handlebody. In all of these situations the space T of marked objects has a partial compactification Tbar with a `` boundary complex" that encodes the structure of Tbar - T. These boundary complexes are, respectively, the curve complex of a surface, the disc complex of a handlebody and the simplicial closure of Outer space. In joint work with R. Ramadas, R. Silversmith and R Winarski we fill in the details of this picture, some of which are classical but many of which are new for surfaces and handlebodies with labelled points and graphs with leaves. We also argue that the cone on the boundary complex is a good candidate for the ``tropicalization" of the space of marked objects.

#### Dessislava Kochloukova, State University of Campinas Weak commutativity, virtually nilpotent groups, and Dehn functions

We will discuss some recent results (joint with Martin Bridson) on the weak commutativity construction X(G). This includes the fact that when G is finitely presented the group X(G) is finitely presented too. We will show that under some conditions X(G) satisfies polynomial isoperimetric inequalities.

#### Richard Schwartz, Brown The optimal paper Moebius band

I will explain why you can twist a 1 x L rectangular strip of paper in space and glue the ends together to make an embedded Moebius band if and only if L exceeds the square root of three. This result was conjectured by B. Halpern and C. Weaver in 1977. I'll also discuss some further developments and conjectures related to optimal paper geometry.

### Thursday, 3 July

#### Ian Agol, UC Berkeley Hyperbolic lattices as automorphism groups

We prove that a non-arithmetic lattice in PSL(2,C) is an automorphism group of a finite-index subgroup. This question is motivated by possible applications to profinite rigidity. Some generalizations will also be considered. This is joint work with Tam Cheetham-West and Yair Minsky.

#### Anne Thomas, Sydney

#### **Reflections, cubulations and Kazhdan-Lusztig polynomials**

Let W be any Coxeter group, with Coxeter generating set S. This means that W is generated by S, so that  $s^2 = 1$  for all  $s \in S$ , and all other relations are of the form  $(st)^m = 1$ . A reflection in W is a conjugate of an element of S. There is a partial order on the elements of W, called Bruhat order, which involves both S-length and reflections. This partial order is very important in the combinatorial theory of Coxeter groups and its applications in representation theory.

For example, the Combinatorial Invariance Conjecture, which was formulated by Lusztig and Dyer in the 1980s, says that the Kazhdan-Lusztig polynomial  $P_(x, y)$  indexed by a pair of elements  $x, y \in W$ , with  $x \le y$  in Bruhat order, is completely determined by the poset structure of the interval [x, y]. I will present a connection between the poset [e, y] being cubulated, in a sense I will define, and  $P_(x, y) = 1$  for all  $x \le y$ . The proofs use normal forms and volume growth series for W, and I will not assume any knowledge of Kazhdan-Lusztig polynomials. This is joint work with Alex Bishop and Elizabeth Milićević.

#### Kasia Jankiewicz, UC Santa Cruz Cubical quotients of cubical nonproducts

Burger-Mozes constructed examples of simple groups acting geometrically on a CAT(0) complex, which is a product of trees. As a counterpoint, we prove that every group acting geometrically on a CAT(0) cube complex which is not a product, admits a nontrivial quotient which also admits a geometric action on a CAT(0) cube complex. Our construction relies on the cubical version of small cancelation theory. This is joint work with M. Arenas and D. Wise.

#### Richard Wade, Oxford Duality for Cohen-Macaulay complexes and the top dimensional cohomology of Out(F\_N)

The thick part of Teichmüller space is a manifold with boundary, which allows one to use Poincaré duality to study the dualizing module of the mapping class group (in the sense of group cohomology).

Although Outer space is not a manifold, it is a Cohen-Macaulay complex. In joint work with Wasserman, we described how Cohen-Macualay complexes satisfy certain (weakened) versions of Poincaré duality, and used this to get a very coarse bound on the dimension of the rational cohomology of Out(F\_n) in the vcd.

The bound is not easy to compute and is given in terms of the representation theory of the action of the hyperoctohedral group on the link of a rose in Outer space. However, we will shed light on the situation when n=3 by consulting work of Bridson.

### Tatiana Nagnibeda, GenevaGroups acting on rooted trees and their subgroups

The class of groups acting by automorphisms on infinite rooted regular trees contains many examples of groups with exotic properties, like groups of intermediate growth, infinite finitely generated torsion groups, amenable but not elementary groups. Moreover, it contains interesting sub-classes of groups like branch groups or self-similar groups. We will discuss the structure of finitely generated subgroups in certain branch selfsimilar groups, their LERF property and its various reinforcements, application to the study of maximal subgroups and, if time permits, some results on decision problems for these groups.

### Friday, 4 July

#### Pierre-Emmanuel Caprace, UC Louvain Some BMW groups I have known

BMW groups are groups acting regularly on the vertices of the Cartesian product of two trees. They include the groups that factorize as a (possibly non direct) product of two free groups.

They are named after Burger-Mozes and Wise, who pioneered their study and revealed their importance in geometric group theory, notably by constructing various examples with striking properties (arithmeticity, non-residual finiteness, virtual simplicity).

The goal of this talk is to present an overview of this class of groups, based on a selection of explicit examples. I will emphasize that, in some cases, valuable information on the structure of a BMW group can be detected in a single finite quotient.

### Jean Pierre Mutanguha, McGill *Canonical decompositions of free-by-cyclic groups*

Free-by-cyclic groups can be defined as mapping tori of free group automorphisms. I will discuss a dynamical decomposition of automorphisms that produces a canonical decomposition of the corresponding free-by-cyclic groups. This will involve the partial order on attracting laminations for an automorphism. The decomposition of free-by-cyclic groups can be considered an extension of the JSJ decomposition of 3manifolds. This talk is on joint work with Spencer Dowdall, Yassine Geurch, Radhika Gupta, and Caglar Uyanik.

#### Wolfgang Lück, Bonn *K-theory, groups, and geometry*

We give a gentle and brief introduction to the lower and middle K-groups of the integral group ring of a group and discuss the conjecture that they all vanish for torsionfree groups. This together with some information about L-groups has a lot of implications to questions and problems in group theory, geometry, and topology, e.g., it implies the conjectures due to Bass, Borel, Gromov, Kaplansky, Novikov, Wall, and Serre about topological rigidity of aspherical closed manifolds, boundaries of hyperbolic groups, idempotents in group rings, Poincare duality groups, and so on.

On the other hand methods from geometric group theory play a key role in the proof of this conjecture which is known to be true for a large class of groups including hyperbolic groups, finitedimensional CAT(0)-groups, and lattices. We are aware that this is the last talk of the conference and therefore will emphasise easy to formulate results and try to give an intriguing panorama, but no technical details. Finally we make some comments on fibering.